

Section 3.4: Simplex Method

- Linear programming problem standard form, introducing slack variables, constructing simplex tableau.
- pivot column, pivot row, and pivot element for a given simplex tableau.
- basic and non-basic variables, optimal solution, leftovers.
- Use technology to perform pivots on a simplex tableau to put the tableau in final form.
- Pr 1. Determine if the following linear programming problems are standard maximization problems. If they are, then convert the constraints of the linear programming problem to linear equations with slack variables, and right down the corresponding tableau.

(a)

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maximize P = 2x + y
subject to: 2y \le 9 - x
8 - y \le x
x \ge 0, y \ge 0
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(b)

Maximize
$$R = y - x$$

subject to: $3y \le 18 - 2x$
 $y - 2x + 10 \ge 0$
 $x \ge 0, y \ge 0$

Pr 2. For the following simplex tableau, identify the pivot row, pivot column, and pivot element. $\begin{bmatrix} x & y & s_1 & s_2 \\ x & y & s_1 & s_2 \end{bmatrix}$ constant

	x	y	s_1	s_2	P	$\operatorname{constant}$
(a)	0	2	1	0	0	8
	1	$\frac{1}{2}$	0	$\frac{1}{2}$	0	5
	0	$\frac{-1}{2}$	0	$\frac{3}{2}$	1	15

(b)
$$\begin{bmatrix} x & y & s_1 & s_2 & P & \text{constant} \\ 1 & 0 & 1 & 0 & 0 & 8 \\ -1 & 1 & 0 & 1 & 0 & 0 \\ \hline -2 & -3 & 0 & 0 & 1 & 0 \end{bmatrix}$$

(c)
$$\begin{bmatrix} x & y & z & s_1 & s_2 & P & \text{constant} \\ 0 & 2 & 1 & 0 & 0 & 0 & 8 \\ 1 & \frac{1}{2} & 0 & \frac{1}{3} & 0 & 0 & 5 \\ \hline 0 & \frac{1}{2} & 0 & 2 & \frac{3}{2} & 1 & 15 \end{bmatrix}$$

Pr 3. For the following simplex tableau, identify the basic and non-basic variables. State the solution corresponding to the tableau, and determine if it is an optimal solution. $\begin{bmatrix} x & y & s_1 & s_2 & P \ | \text{ constant } \end{bmatrix}$

	x	y	s_1	s_2	P	$\operatorname{constant}$
(a)	0	2	1	0	0	8
	1	$\frac{1}{2}$	0	$\frac{1}{2}$	0	5
	0	$\frac{-1}{2}$	0	$\frac{3}{2}$	1	15

	x	y	s_1	s_2	P	constant
(b)	1	0	1	0	0	8
	-1	1	0	1	0	0
	-2	-3	0	0	1	0

	x	y	z	s_1	s_2	P	constant	
(c)	0	2	1	0	0	0	9	
	1	$\frac{1}{2}$	0	$\frac{1}{3}$	0	0	2	
	0	$\frac{1}{2}$	0	2	$\frac{3}{2}$	1	42	

Pr 4. Solve.

An independent taffy company makes three flavors of taffy: strawberry, lemon, and orange. Each strawberry taffy requires 4 minutes to cool and 1 minute to wrap in paper. Each orange taffy requires 3 minutes to cool and 1.5 minutes to wrap in paper. Each lemon taffy requires 4 minutes to cool and 2 minutes to wrap in paper. There are a total of 1.5 hours available for cooling and 0.5 hours available for wrapping. Determine the production of each taffy to maximize profit if the profit on the sale of each orange, lemon, and strawberry taffy is 75 cents, 60 cents, and 50 cents, respectively, and previous sales indicate that they should produce at least three times as many strawberry taffy as lemon taffy. How many of each flavor should the company make to maximize their profits? What is the maximum profit and is any time leftover in cooling or wrapping?

Section 4.1: Mathematical Experiments

- $\bullet\,$ Sample space, ${\bf S}$ a list of all possible outcomes in the mathematical experiments
- Event a subset of the sample space
 - Simple Event
 - Certain Event
 - Impossible Event
- Using tree diagrams to determine a sample space in a two-stage experiment
- Venn Diagrams
- Operations on Events
 - Complement, A^C
 - Intersection, $A \cap B$
 - Union, $A\cup B$
- Mutually Exclusive Events
- **Pr 1.** State the sample space for each experiment:
 - (a) Selecting a letter at random from the word "math" and noting the letter.
 - (b) Identical ping pong balls are numbered 0 to 10, one ping pong ball is drawn at random, noting the number on the ball.
 - (c) A standard 20-sided die is rolled and it is noted whether the number is a multiple of 3 or is not a multiple of 3.
 - (d) The numbers 0, 1,2, 3, and 4 are written on separate pieces of paper and put in a hat. Two pieces of paper are drawn at the same time and the product of the numbers is noted.
 - (e) A card is drawn from a standard deck of 52-cards, noting the suit, and then a fair coin is flipped, noting whether it lands on heads or tails.

- Pr 2. Consider the experiment of selecting a letter at random from the word "math" and noting the letter.(a) State all the simple events for the experiment.
 - (b) State the certain event for the experiment.
 - (c) Give an example of an impossible event for the experiment.
 - (d) State the total number of possible events.
 - (e) Write the outcomes in the event, J, "a consonant is draw."
- Pr 3. A card is drawn from a standard deck of 52-cards, noting the suit, and then a fair coin is flipped, noting the coin lands on heads or tails.
 - (a) State all the simple events for the experiment.
 - (b) State the certain event for the experiment.
 - (c) Give an example of an impossible event for the experiment.
 - (d) State the total number of possible events.
 - (e) Write the outcomes in the event, M, "a diamond is drawn or the coin lands on heads."

 $\label{eq:pr_state} \mathbf{Pr} \ \ \mathbf{4.} \ \ \mathrm{Let} \ A \ \mathrm{and} \ B \ \mathrm{be} \ \mathrm{two} \ \mathrm{events} \ \mathrm{of} \ \mathrm{the} \ \mathrm{sample} \ \mathrm{space}, \ \mathrm{S}.$

Use a two-circle Venn diagram to illustrate which region(s) contain the outcomes of the resulting events. a. $B^C \cap A$



b. $(A \cup B) \cap A^C$



S

B

A

c.
$$(A^C \cup B)^C$$

- **Pr** 5. An experiment consists of rolling a four-sided die, noting the number showing uppermost and then spinning a spinner with four equal regions (red, white, blue, and maroon), noting the color.
 - Let
 - V := the event "a number greater than 3 is rolled"
 - W:= the event "an even is rolled"
 - X := the event "the spinner lands on blue"
 - Y := the event "the spinner lands on a color other than maroon"
 - Z := the event "the spinner lands on white or maroon."
 - (a) Write the symbolic notation for the event, D, that "an odd is rolled or the spinner lands on white or maroon."

(b) Write the symbolic notation for the event, H, that "a number less than or equal to 3 is rolled or the spinner lands on a color other than maroon, but not blue."

(c) Describe the event $X^C \cap W$.

(d) Describe the event $Z \cup Y \cup Y^C$

(e) Are event V and event W mutually exclusive? Explain why or why not.