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1 Week 12 HOGU: 5.5-5.8, Exam 3 Review

Problem 1. Find the domain of each of the following functions. Draw the domain on the number line, then give your answer using interval notation.

(a)
$$f(x) = \begin{cases} 3x^2 - 4 & \text{if } x < 8\\ 7 & \text{if } x = 8\\ \sqrt[4]{x - 4} & x > 8 \end{cases}$$

(b)
$$g(x) = \begin{cases} \frac{\sqrt[3]{2x - 15}}{x} & \text{if } x \le 1\\ \frac{9}{\sqrt{x - 2}} & \text{if } x > 1 \end{cases}$$

Problem 2. Your electric bill came in! On your bill you noticed that you were charged \$7 as a base fee, plus \$6 per kilowatt-hour of electricity used up to the first 100 kilowatt-hours. (These numbers were taken from my own electric bill!) After using 100 kilowatt-hours, you notice that the amount you are charged goes up to \$9 per kilowatt-hour. Construct the piecewise function describing the cost C(x), in dollars, that you pay when using x kilowatt-hours of electricity.

Problem 3. State the domain of the following functions:

(a)
$$f(x) = 4e^{x-1}$$

(b)
$$g(x) = \ln(1-x)$$

(c)
$$k(x) = \frac{\sqrt{x^3 + 8}}{\ln(x)}$$

Problem 4. (a) Completely simplify this expression to be in base 6:

$$\frac{36^{x^2}}{6^{-4x}}$$

(b) Fully expand the expression using the properties of logarithms:

$$\ln\left(\sqrt[3]{\frac{x^3}{e^2z^4}}\right).$$

Problem 5. Solve the following equations for x:

(a)
$$4^{x+1} = 64$$

(b)
$$\ln(x) + \ln(x-2) = \ln(x+10)$$

(c)
$$2 \cdot 3^{-x} = 16$$

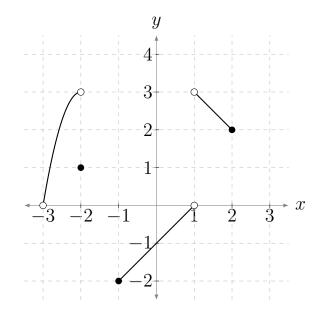
Problem 6. Recall that the accumulated value of an initial deposit, P, for t years, at the interest rate r (expressed as a decimal), is

$$A(t) = P\left(1 + \frac{r}{m}\right)^{mt},$$

where m represents the number of times the interest is compounded in a year.

If you deposit \$12,000 in this savings account and the interest rate on the account is 7%, how long would it take the savings account to grow to \$25,000? Assume that interest is compounded yearly.

Problem 7. Consider the function f(x) below:



(a) State the domain of f(x). Write your answer in interval notation.

(b) State the range of f(x). Write your answer in interval notation.

Problem 8. Compute and completely simplify the difference quotient for the function $g(x) = -\frac{3}{x+1}$.

(a)
$$g(x+h) =$$

(b) g(x+h) - g(x) =

(c)
$$\frac{g(x+h) - g(x)}{h} =$$

Problem 9. Compute and completely simplify the difference quotient for the function $k(x) = \sqrt{2x-5}$.

(a)
$$k(x+h) =$$

(b) k(x+h) - k(x) =

(c)
$$\frac{k(x+h) - k(x)}{h} =$$