## Math 251/221

## WEEK in REVIEW 7.

1. Evaluate the integral  $\iiint_E (xy+z^2)dV$ , where  $E = [0,2] \times [0,1] \times [0,3]$ .

2. Evaluate the iterated integral  $\int_0^2 \int_0^{z^2} \int_0^{y-z} (2x-y) \, dx \, dy \, dz$ 

- 3. Express the integral  $\iiint_E f(x, y, z) dV$  as an iterated integral in six different ways, where E is the solid bounded by the surfaces  $y = x^2$ , z = 0, y + 2z = 4.
- 4. Evaluate the triple integral
  - (a)  $\iiint_{E} e^{z/y} dV$ , where  $E = \{(x, y, z) : 0 \le y \le 1, y \le x \le 1, 0 \le z \le xy\}$
  - (b)  $\iiint_E 6xy \, dV$ , where E lies under the plane z = 1 + x + y and above the region in the xy-plane bounded by the curves  $y = \sqrt{x}$ , y = 0, and x = 1.
  - (c)  $\iiint_E x \, dV$ , where E is bounded by a paraboloid  $x = 4y^2 + 4z^2$  and the plane x = 4.
  - (d)  $\iiint_E z \, dV$ , where E is bounded by the cylinder  $y^2 + z^2 = 9$  and the planes x = 0, y = 3x, and z = 0 in the first octant.
- 5. Use a triple integral to find the volume of the region bounded by the parabolic cylinders  $z = x^2$ ,  $z = 2 x^2$ and by the planes y = 0, y + z = 4.
- 6. Write the equation  $x^2 + y^2 + z^2 = 4y$  in cylindrical and spherical coordinates.
- 7. Convert the integral

$$\int_0^1 \int_0^{\sqrt{1-y^2}} \int_{x^2+y^2}^{\sqrt{x^2+y^2}} xyz \, dz \, dx \, dy$$

to an integral in cylindrical coordinates, but don't evaluate it.

8. Convert the integral

$$\int_0^3 \int_0^{\sqrt{9-y^2}} \int_0^{\sqrt{9-x^2-y^2}} (x^2 + y^2 + z^2) \, dz \, dx \, dy$$

to an integral in spherical coordinates, but don't evaluate it.

- 9. Use cylindrical and spherical coordinates to find the volume of the ice-cream cone bounded above by the sphere  $x^2 + y^2 + z^2 = 5$  and below by the cone  $z = 2\sqrt{x^2 + y^2}$ .
- 10. Let E be the solid region bounded below by the cone  $z^2 = x^2 + y^2$ ,  $z \ge 0$  and above by the plane z = 4. Set up the integral for computing the mass of the solid if the density is  $\rho(x, y, z) = xyz$  in
  - (a) cylindrical coordinates
  - (b) spherical coordinates