



Example 1 (12.1). *Let P , Q , and R be the projections of the point $S(3, 5, 7)$ onto xy -plane, yz -plane and xz -plane, respectively. Determine the coordinates of the points P, Q , and R , and compute the distance from the origin to the point S .*

Example 2 (12.1). (a) *Sketch the graph of $x^2 + y^2 = 9$ in \mathbb{R}^2 .*

(b) *Sketch the graph of $x^2 + y^2 = 9$ in \mathbb{R}^3 .*

(c) *Sketch the graph of $y^2 + z^2 = 1, x \geq 2$ in \mathbb{R}^3 .*



Example 3 (12.1). Let the sphere S_1 is given by the equation $x^2 + y^2 + z^2 + 2x - 4z = 11$. Find the distance between the center of the sphere S_1 and the point $P(1, 4, 6)$.

Example 4 (12.2). The initial point of a vector \mathbf{v} in \mathbb{R}^2 is the origin and the terminal point is in the quad II. If \mathbf{v} makes an angle of $\frac{2\pi}{3}$ with positive x -axis and $|\mathbf{v}| = 6$, find the vector \mathbf{v} .

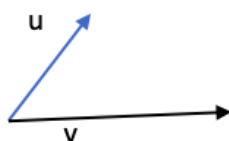


Example 5 (12.2). *Draw the vectors as described below.*

$3\mathbf{v}$ and $-2\mathbf{v}$



$\mathbf{u} + \mathbf{v}$



$\mathbf{u} + \mathbf{w}$ and $\mathbf{u} - \mathbf{w}$



Example 6 (12.2). *Find the unit vectors that are parallel to the tangent line to the parabola $y = x^2$ at the point $(4, 16)$.*



Example 7 (12.3). *If $\mathbf{a} = \langle 2, -1, 0 \rangle$, find a vector \mathbf{b} such that $\text{comp}_{\mathbf{a}}\mathbf{b} = 3$.*

Example 8 (12.3). *Find the direction angles of the vector $\mathbf{a} = \langle 1, 2, -1 \rangle$.*



Example 9 (12.3). Use vectors to determine whether the triangle with vertices $A(3, 2, 0)$, $B(0, 1, 2)$ and $C(3, 1, 2)$ is right-angled.

Example 10 (12.3). Consider the triangle below is an equilateral triangle with $|\mathbf{u}| = 1$. Compute $\mathbf{u} \cdot \mathbf{v}$ and $\mathbf{u} \cdot \mathbf{w}$.

