

1. Evaluate the integral

a) $\int_0^{\pi/12} \sin(3x - 2) dx$

b) $\int x(4x^2 + 1)^6 dx$

c) $\int x^3(x^2 + 3)^3 dx$

d) $\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$

e) $\int_0^1 x^2 e^{x^3} dx$

f) $\int \frac{x + \arcsin x}{\sqrt{1 - x^2}} dx$

g) $\int \frac{2x^2 + 4x}{x^3 + 3x^2 - 4} dx$

h) $\int \frac{e^x}{e^x + 1} dx$

i) $\int_e^{e^4} \frac{dx}{x\sqrt{\ln x}}$

j) $\int \frac{x dx}{\sqrt{1 + x^4}}$

k) $\int_1^4 \frac{1}{x^2} \sqrt{\frac{1}{x} + 1} dx$

l) $\int \tan x \ln(\cos x) dx$

2. Sketch the region bounded by the given curves and find the area of the region.

(a) $y = x^2 + 2$, $y = 2x + 5$, $x = 0$, $x = 6$.

(b) $y = \cos x$, $y = \sin 2x$, $x = 0$, $x = \pi/2$.

(c) $x + y^2 = 2$, $x + y = 0$.

3. Find the area of the triangle with vertices $(0, 0)$, $(3, 1)$, $(6, -6)$.

4. Find the volume of the solid S whose base is a region bounded by the parabola $y = 1 - x^2$ and the x -axis, and cross sections perpendicular to the y -axis are equilateral triangles.

5. Find the volume of the solid S whose base is the triangular region with vertices $(0, 0)$, $(2, 0)$, $(0, 1)$, and cross sections perpendicular to the x -axis are semicircles.

6. Set up the integrals to find the volume of the solid obtained by rotating the region bounded by the curves $y = 4 - x^2$, $y = 1$, $x = 1$, $x = 2$ about the indicated lines using the method of disks/washers.

(a) about the line $y = 1$

(b) about the x -axis

(c) about the line $y = 5$

(d) about the line $y = -3$

(e) about the line $y = 0.5$

- (f) about the line $x = 1$
- (g) about the y - axis
- (h) about the line $x = 2$
- (i) about the line $x = 5$
- (j) about the line $x = -2$
- (k) about the line $x = 0.5$