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# MATH 150 - WEEK-IN-REVIEW 10

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## PROBLEM STATEMENTS

- Given  $\sin(\theta) = -\frac{5}{7}$  and  $\tan(\theta) > 0$ , find  $\tan(\theta)$  and  $\sec(\theta)$ .

- Use the function value to find the indicated trigonometric value in the specified quadrant.

**Function Value:**  $\sec \theta = -\frac{61}{11}$     **Quadrant:** III    **Trigonometric Function:**  $\cot \theta$

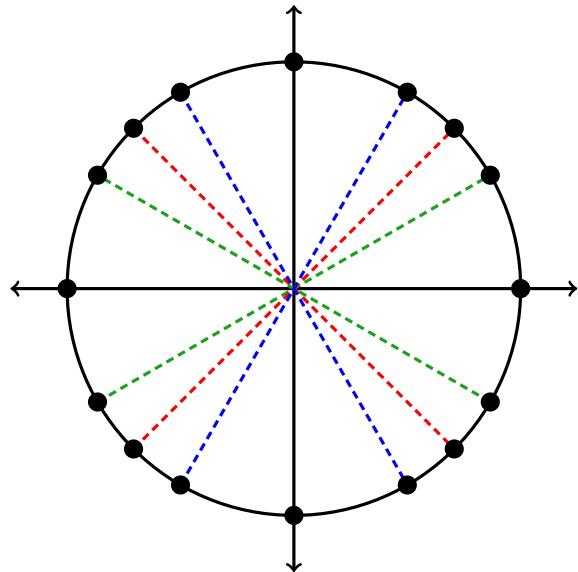
3. Given  $\sin \theta = \frac{4}{7}$  and  $\theta$  in Quadrant I, use the trigonometric identities to find the exact value of each:

a.  $\cos(\theta) =$

b.  $\cot(\theta) =$

c.  $\csc(\theta) =$

d.  $\tan(90^\circ - \theta) =$



4. Evaluate the following:

a)  $\sin \frac{4\pi}{3}$

a)  $\sin 315^\circ$

b)  $\cos \frac{4\pi}{3}$

b)  $\cos 315^\circ$

c)  $\tan \frac{4\pi}{3}$

c)  $\tan 315^\circ$

d)  $\cot \frac{4\pi}{3}$

d)  $\cot 315^\circ$

e)  $\sec \frac{4\pi}{3}$

e)  $\sec 315^\circ$

f)  $\csc \frac{4\pi}{3}$

f)  $\csc 315^\circ$

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5. Given  $y = 3 \sin(4x + \pi)$ , describe the period, amplitude, and phase shift of the graph. Then graph the function.

Amplitude:

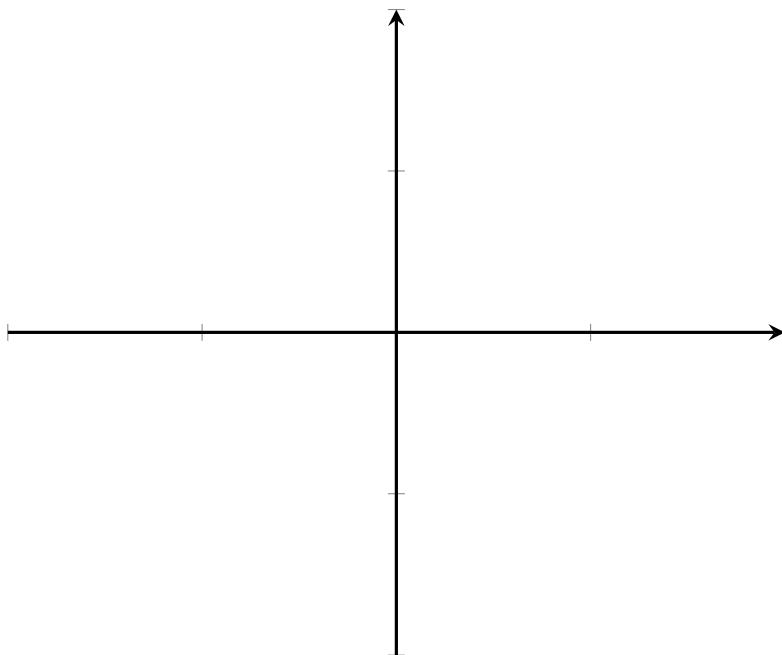
**Period Endpoints**

Start:

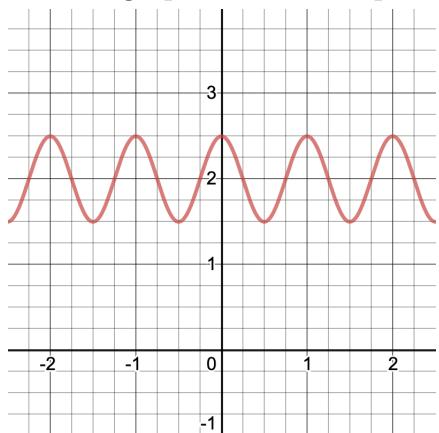
End:

Period:

Phase Shift:



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6. Given the graph, write the equation of the cosine function which matches the graph.



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7. Graph one cycle of the function  $y = 1 + \sec\left(\frac{t}{2}\right)$  and state its period.

8. Evaluate each:

a. $\arcsin\left(\frac{\sqrt{2}}{2}\right) =$ b. $\arcsin(3) =$ c. $\arcsin\left(-\frac{\sqrt{3}}{2}\right) =$ d. $\arcsin(-1) =$	a. $\arccos\left(-\frac{\sqrt{2}}{2}\right) =$ b. $\arccos\left(\frac{1}{2}\right) =$ c. $\arccos(1) =$ d. $\arccos(-2) =$
a. $\arctan\left(-\sqrt{3}\right) =$ b. $\arctan(3) =$ c. $\arctan(-1) =$ d. $\arctan\left(\frac{5}{2}\right) =$	<b>Reminders:</b> <ul style="list-style-type: none"> <li>• Domain <math>\arcsin x = [-1, 1]</math>, Range <math>\arcsin x = \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]</math></li> <li>• Domain <math>\arccos x = [-1, 1]</math>, Range <math>\arccos x = [0, \pi]</math></li> <li>• Domain <math>\arctan x = (-\infty, \infty)</math>, Range <math>\arctan x = \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)</math></li> </ul>

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9. Evaluate each of the following:

(a)  $\arccos \left( \sin \left( \frac{11\pi}{6} \right) \right)$

(b)  $\arccos \left( \sin \left( \frac{3\pi}{4} \right) \right)$

(c)  $\sin \left( \arctan \left( -\frac{\sqrt{3}}{3} \right) \right)$

(d)  $\cos \left( \arcsin \left( -\frac{8}{17} \right) \right)$

(e)  $\cos(\arccos(2))$

10. Write an algebraic expression that is equivalent to:

a.  $\tan(\arcsin(5x))$

b.  $\csc\left(\arccos\left(\frac{x}{2}\right)\right)$ .

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11. Find all solutions to  $\sqrt{3} \csc(x) + 3 = 1$  then state the solutions that are in the interval  $[0, 2\pi)$ .
12. Find all solutions to the equation  $2 \sin^2(3x) - 1 = 0$  then state the solutions that are in the interval  $[0, \pi)$ .

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13. Find all solutions for  $80 \cos\left(\frac{\pi}{3}x + \frac{\pi}{4}\right) - 40\sqrt{2} = 0$  then state the solutions that are in the interval  $[0, 5)$ .