

1. Write the correct partial fraction expansion. Do not solve for unknown constants.

a)
$$\frac{x^5 + 2x^4 - x^3 + 3x^2 + x - 1}{x^3 + x^4}$$

b)
$$\frac{x}{x^2 + x - 6}$$

c)
$$\frac{1 + 16x}{(2x - 3)(x^2 + 4)(x + 5)^2}$$

2. Evaluate the integral.

a)
$$\int \frac{5x + 1}{(2x + 1)(x - 1)} dx$$

b)
$$\int \frac{x^2 + x + 1}{(x + 1)^2(x + 2)} dx$$

c)
$$\int \frac{x^2 dx}{x^4 - 81}$$

d)
$$\int \frac{x^2 dx}{\sqrt{9 - 25x^2}}$$

e)
$$\int \frac{x^5 - x^4 - 2x^2 + 2x + 5}{x^4 + x^3} dx$$

3. Evaluate the improper integral or show that it is divergent.

a)
$$\int_{-\infty}^{\infty} \frac{dx}{x^2 + 25}$$

b)
$$\int_0^{\infty} \frac{dx}{(x + 2)(x + 3)}$$

c)
$$\int_1^{\infty} \frac{\ln x}{x^3} dx$$

d)
$$\int_{\pi/4}^{\pi/2} \tan^2 x dx$$

e)
$$\int_3^{10} \frac{dx}{x^2 - 9}$$

f)
$$\int_1^{\infty} \sin(\pi x) dx$$

g)
$$\int_0^5 \frac{dx}{x - 5}$$

4. Use the Comparison Test to determine whether the following integral is divergent or convergent.

a)
$$\int_1^{\infty} \frac{dx}{\sqrt[3]{x^3 + 1}}$$

b)
$$\int_1^{\infty} \frac{\cos^2 x}{x^2} dx$$

c)
$$\int_1^{\infty} \frac{2 + \cos x}{\sqrt{x^4 + x^2}} dx$$

d)
$$\int_1^{\infty} \frac{1 + e^{-x}}{x} dx$$