

Problem 1

Suppose X is a continuous random variable. If P (X \ge 16) = 0.03, then

1. P(X < 16) =2. $P(X \le 16) =$ 3. P(X > 16) =4. P(X=16) =



Problem 2

Topics: continuous random variables, Normal distribution, empirical rule

۱

Given an approximately normal distribution with a mean of 175 and a standard deviation of 37. Use the empirical rule.

- 5. Draw a normal curve and label 1, 2, and 3 standard deviations on both sides on the mean.
- 6. What percent of values are within the interval (138, 212)?
- 7. What percent of values are within the interval (64, 286)?

Problem 3

Topics: continuous random variables, Normal distribution, empirical rule

It is known that when a specific type of radish is grown in a certain manner without fertilizer the weights of the radishes produced are normally distributed with a mean of 40g and a standard deviation of 10g.

Determine the proportion of radishes grown. Use the empirical rule.

- 1. Without fertilizer with weights less than 50 grams.
- 2. Without fertilizer with weights between 20 and 60 grams.
- 3. Without fertilizer that will have weights greater than or equal to 60 grams.



Problem 4:

Topics: continuous random variables, Normal distribution, empirical rule

- 4. Which of the following would indicate that a dataset is **not** bell-shaped³?
 - a. The range is equal to 5 standard deviations.
 - b. The range is larger than the interquartile range.
 - c. The mean is much smaller than the median.
 - d. There are no outliers.
 - e. None of the above

Problem 5

5. What is the z-score of x = 5 if it is 1.8 standard deviations below the mean?

Problem 6:

Topics: continuous random variable, standard normal distribution, probability, use of the Z table

- 6. What percent of a standard normal distribution N(μ =0, σ = 1) is found in each region? <u>Be sure to draw a graph</u>
 - a. Z < 1.35
 b. Z > 1.48
 c. 0.4 < Z < 1.5
 d. Z < -20.92 or Z > 20.97

Problem 7:

 Using the standard normal distribution, find the two z-scores that form the middle shaded region. The shaded region is symmetric about z = 0, Round your zscores to two decimal places.





Problem 8:

Topics: histogram, Normal approximation to data, Normal probability plot, Q-Q plot

8. Can we approximate poker winnings by a normal distribution? We consider the poker winnings of an individual over 50 days. A histogram and normal probability plot of these data are shown in the following figure⁴:



Figure 3.13: A histogram of poker data with the best fitting normal plot and a normal probability plot.

Problem 9

 Overweight baggage. Suppose weights of the checked baggage of airline passengers follow a nearly normal distribution with mean 45 pounds and standard deviation 3.2 pounds. Most airlines charge a fee for baggage that weigh in excess of 50 pounds⁴. Determine what percent of airline passengers incur this fee.



Problem 10

The cholesterol content of large chicken eggs is normally distributed with a mean of 200 milligrams and standard deviation 15 milligrams.

- 10. What is the probability that the cholesterol content of a random egg is less than 205 milligrams?
- 11. In sixty-seven percent of the eggs, the cholesterol content is less than a certain value "C".

Find the value of "C".

a) 0.33 b) 206.6 c) 210 d) 0.44 e) 193.4

Problem 11

Topics: Normal distribution, parameters of the normal distribution, z-score, quartiles, use of the Z table

Auto insurance premiums. Suppose a newspaper article states that the distribution of auto insurance premiums for residents of California is approximately normal with a mean of \$1,650. The article also states that 25% of California residents pay more than \$1,800.

- 12. What is the z-score that corresponds to the top 25% of the standard normal distribution?
- 13. What is the mean insurance cost? What is the cutoff for the 75th percentile?
- 14. Identify the standard deviation of insurance premiums in LA.