

1. Find the limit.

(a) $\lim_{t \rightarrow 0} \frac{\sin^2 3t}{t^2}$

(b) $\lim_{x \rightarrow 0} \frac{\sin 3x}{\sin 5x}$

(c) $\lim_{x \rightarrow 0} \frac{(\cos x - 1) \sin 3x}{x^2}$

(d) $\lim_{x \rightarrow -2} \frac{\tan \pi x}{x + 2}$

2. Differentiate the function.

(a) $s(t) = t^8 + 6t^7 - 18t^2 + 2t$

(b) $x(t) = \sqrt[3]{t} - \frac{1}{\sqrt[3]{t}}$

(c) $f(x) = (3x^3 - 2x^2 + 1)^6$

(d) $G(x) = \frac{3x - 7}{x^2 + 5x - 4}$

(e) $f(x) = \sqrt{x^3 - 3x^2 + 3x - 1}$

(f) $g(\theta) = (1 + \cos^2 \theta)^3$

(g) $f(x) = \cos \sqrt{x}$

(h) $f(x) = \left(\frac{x^4 - 1}{x^4 + 1} \right)^3$

(i) $f(x) = \frac{2x + 1}{\sqrt{x^2 + 3}}$

(j) $f(x) = (x^6 + 4x^5 - 11)^5 (2 + x^8)^7$

3. Functions f and g satisfy the properties as shown in the table. Find the indicated quantity.

| x | $f(x)$ | $f'(x)$ | $g(x)$ | $g'(x)$ |
|-----|--------|---------|--------|---------|
| 1 | -3 | 3 | 1 | 1 |
| 2 | 0 | 3 | -5 | 10 |
| 3 | 2 | 5 | 0 | 4 |

(a) $h'(1)$, if $h(x) = f(g(x))$

(b) $z'(2)$, if $z(x) = [f(2x - 1)]^4$

(c) $G'(1)$, if $G(x) = [x^2 - g(2x)]^3$

4. For what values of x does the graph of $f(x) = 2x^3 - 3x^2 - 6x + 87$ have a horizontal tangent?

5. Find the equation of the tangent line to the curve $y = x\sqrt{1+x^2}$ at the point where $x = 1$.

6. Find $\frac{dy}{dx}$ for the equation $\cos(x - y) = y \sin x$.

7. Find $\frac{dx}{dy}$ for the equation $y^4 + x^2 y^2 + y x^4 = y + 1$.

8. Find the slope of the tangent line to the curve $2(x^2 + y^2)^2 = 25(x^2 - y^2)$ at the point $(3, 1)$.